

Given that  $x = \frac{2}{\cos\theta}$  and  $y = 3\tan\theta$

Show that  $\frac{x^2}{4} - \frac{y^2}{9} = 1$

a)

$$\frac{x^2}{4} - \frac{y^2}{9} = \frac{\left(\frac{2}{\cos\theta}\right)^2}{4} - \frac{(3\tan\theta)^2}{9}$$

$$\frac{x^2}{4} - \frac{y^2}{9} = \frac{4}{\cos^2\theta} - \frac{9\tan^2\theta}{9}$$

$$\frac{x^2}{4} - \frac{y^2}{9} = \frac{4}{4\cos^2\theta} - \tan^2\theta$$

$$\frac{x^2}{4} - \frac{y^2}{9} = \frac{1}{\cos^2\theta} - \tan^2\theta$$

$$\frac{x^2}{4} - \frac{y^2}{9} = \frac{1}{\cos^2\theta} - \frac{\sin^2\theta}{\cos^2\theta}$$

$$\frac{x^2}{4} - \frac{y^2}{9} = \frac{1 - \sin^2\theta}{\cos^2\theta}$$

$$\cos^2\theta + \sin^2\theta \equiv 1$$

$$\cos^2\theta \equiv 1 - \sin^2\theta$$

$$\frac{x^2}{4} - \frac{y^2}{9} = \frac{1 - \sin^2\theta}{1 - \sin^2\theta}$$

$$\frac{x^2}{4} - \frac{y^2}{9} = 1$$