

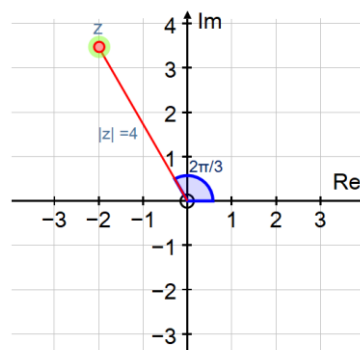
$$z = -2 + 2\sqrt{3}i$$

a) Find $|z|$ and $\arg(z)$

b) Find z^6 and simplify your answer

c) Given that $w^4 = z^3$, find the values of w in the form $a + ib$

a) $z = -2 + 2\sqrt{3}i$



$$|z| = \sqrt{(-2)^2 + (2\sqrt{3})^2}$$

$$|z| = \sqrt{4 + 12} = \sqrt{16}$$

$$|z| = 4$$

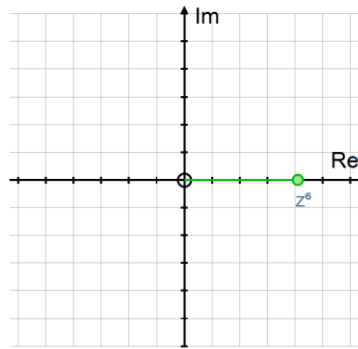
$$\arctan\left(\frac{2\sqrt{3}}{-2}\right) = -\frac{\pi}{3}$$

$$\arg(z) = \frac{2\pi}{3}$$

b) $z = 4\text{cis}\left(\frac{2\pi}{3}\right)$

$$z^6 = 4^6\text{cis}\left(6 \cdot \frac{2\pi}{3}\right)$$

$$z^6 = 4096cis4\pi$$



$$z^6 = 4096$$

c) $w^4 = z^3 = 4^3 cis\left(3 \cdot \frac{2\pi}{3}\right)$

$$w^4 = 64cis2\pi$$

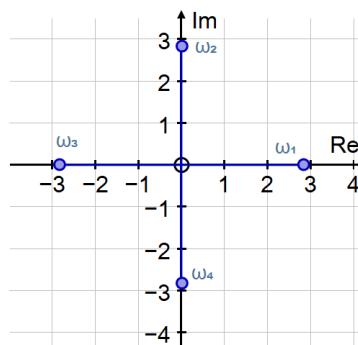
$$w^4 = 64$$

$$w^4 = 64cis(0 + 2k\pi) \quad k = 0,1,2,3$$

$$w = 64^{\frac{1}{4}}cis\left(\frac{2k\pi}{4}\right) \quad k = 0,1,2,3$$

$$w = \sqrt{8}cis\left(\frac{k\pi}{2}\right) \quad k = 0,1,2,3$$

Using symmetry



$$w = \sqrt{8}, \sqrt{8}i, -\sqrt{8}, -\sqrt{8}i$$