

1.10 Systems of Linear Equations

Question Paper

Course	DPIB Maths
Section	1. Number & Algebra
Topic	1.10 Systems of Linear Equations
Difficulty	Very Hard

Time allowed: 90
Score: /72
Percentage: /100

Question 1a

Solve the following simultaneous equations.

(a)

$$\begin{aligned}5x - 2y &= 9.5 \\ -2x - 5y &= 16.5\end{aligned}$$

[2 marks]**Question 1b**

(b)

$$\begin{aligned}3(a - 2b) &= 7 - b \\ 2(2a - b) &= 5b - 11\end{aligned}$$

[2 marks]**Question 1c**

(c)

$$\begin{aligned}\frac{2(p - q)}{5} - \frac{3p}{2} &= \frac{p - 4q}{10} \\ \frac{2p}{3} - \frac{4q}{5} &= 1 - \frac{2}{3}q\end{aligned}$$

[3 marks]

Question 2

Use an algebraic method to solve the following system of linear equations.

$$2x - 3y - 5z = 4$$

$$x - 4y + 6z = -6$$

$$3y - 2x - 3z = 0$$

[6 marks]**Question 3**

Solve the following system of linear equations using an algebraic method.

$$2x - 3y + 4z = -1$$

$$x - 4y - 6z = 8$$

$$5y - 3x - 5z = 1$$

[1 mark]

Question 4

Use an algebraic method to solve the following system of linear equations.

$$3y - 2x + 5z = 14$$

$$3x - 2y - 2z = 11$$

$$3z - 4x - 4y = 35$$

[6 marks]**Question 5**

Find the unique point of intersection of the planes with the following Cartesian equations:

$$x - 3y + 2z = -3$$

$$z + 2y - x = 4$$

$$3z + y - 4x = 1$$

[6 marks]

Question 6

Consider the function f defined by $f(x) = x^4 + ax^3 + bx^2 + cx + 24$. The graph $y = f(x)$ passes through the points $(1, 36)$, $(2, 24)$ and $(3, 0)$.

Find the values of a , b and c .

[6 marks]

Question 7a

Consider the system of equations

$$2a + 6b + xc = y$$

$$6b - a - c = 7$$

$$a + 2b - 3c = 1$$

where x and y are real constants.

(a)

Find the value of x such that the system does not have a unique solution.

[5 marks]

Question 7b

(b)

Given that $c = 0$ find the values of a , b and y such that the system of equations has a solution

[3 marks]

Question 8a

Consider the following system of equations

$$x + 2y - z = 0$$

$$2x - y + 4z = 0$$

$$x - 3y + (1 - a)z = 4 - a^2$$

(a)

Show that the system has a unique solution when $a \neq -4$.

[3 marks]

Question 8b

(b)

For the case where $a \neq -4$, state the solution in terms of a .

[5 marks]

Question 8c

(c)

For the case where $a = -4$, show that there are no solutions.**[2 marks]****Question 9a**

The following system of equations has an infinite number of solutions.

$$3x - 2y - 7z = 3$$

$$2x + y - 4z = 1$$

$$3y - x + 3z = k$$

(a)

Find the value of k .**[4 marks]****Question 9b**

(b)

Find the general solution.

[4 marks]

Question 10a

Consider the following system of linear equations.

$$x - 3y + 3z = k$$

$$3x - 2y + z = 4$$

$$2x + y - 2z = 2$$

(a)

Show that the system of equations does not have a unique solution.

[3 marks]

Question 10b

(b)

Find the value of k for which the equations are consistent.

[2 marks]

Question 10c

(c)

For the value of k found in part (b), find the general solution of these equations.

[3 marks]

Question 11

The rate, R , of increase of the volume of a cloud created in a science lab is related to the change in air temperature, T , and air pressure, P , by the equation

$$R = kT^x P^y, \text{ where } x, y, k \in \mathbb{R}.$$

A meteorologist takes measurements at three intervals and records the data as follows.

Measurement	R (cm^3s^{-1})	T ($^{\circ}\text{C}$)	P (kPa)
1	48.75	17.1	101.2
2	46.13	15.9	101.8
3	43.47	14.7	102.5

Find x , y and k .

[6 marks]

