

# 3.6 Trigonometric Equations & Identities

## Question Paper

Course	DPIB Maths
Section	3. Geometry & Trigonometry
Topic	3.6 Trigonometric Equations & Identities
Difficulty	Hard

**Time allowed:** 80  
**Score:** /60  
**Percentage:** /100

**Question 1a**

The value of  $\tan \alpha = -\frac{3}{2}$  for  $\frac{\pi}{2} \leq \alpha \leq \pi$ .

(a) Find

(i)  $\sin \alpha$

(ii)  $\cos \alpha$

(iii)  $\sin 2\alpha$

(iv)  $\cos 2\alpha$

(v)  $\tan 2\alpha$ .

[7 marks]

**Question 1b**

(b) Use your results from part (a) to explain why  $\pi < 2\alpha < \frac{3\pi}{2}$  must be true.

[2 marks]

**Question 2a**

The value of  $\cos B = x$ , for  $\pi \leq B \leq \frac{3\pi}{2}$ .

(a) Explain why

(i)  $x \leq 0$

(ii)  $\sin B = -\sqrt{1 - x^2}$ .

[3 marks]

**Question 2b**

(b) Hence find the following in terms of  $x$ :

(i)  $\cos 2B$

(ii)  $\sin 2B$

(iii)  $\tan 2B$ .

[5 marks]

**Question 3**

An angle  $M$  is such that  $\sin M = p$  and  $\cos M = q$ . Show that

(i)  $\sin 4M = 4pq^3 - 4p^3q$

(ii)  $\cos 4M = 8q^4 - 8q^2 + 1$ .

[6 marks]

**Question 4**

Solve the equation  $\sqrt{3} \cos 2\theta = 2 \cos^2 2\theta$  in the interval  $0 \leq \theta \leq 360^\circ$ .

**[5 marks]****Question 5**

Solve the equation  $\sqrt{3} \tan x = \frac{1}{\sqrt{3} \tan x}$  for  $0 \leq x \leq 540^\circ$ .

**[5 marks]**

**Question 6a**

(a) Use the fact that

$$16x^3 - 12x^2 - 4x + 3 = (4x - 3)(4x^2 - 1)$$

to fully factorise  $16x^3 - 12x^2 - 4x + 3$ .

[2 marks]

**Question 6b**

(b) Use your result from part (a) to solve the equation

$$16 \sin^3 3\theta - 12 \sin^2 3\theta - 4 \sin 3\theta + 3 = 0$$

in the interval  $0 \leq \theta \leq \frac{\pi}{2}$ . You should give your answers as exact values where possible.

[7 marks]

**Question 7**

Solve the equation

$$\sin^2 x = \frac{\cos x + 4}{6}$$

in the interval  $-\pi \leq x \leq \pi$ . Give your answers as exact values where possible.**[6 marks]**

**Question 8a**

Two functions,  $f$  and  $g$ , are defined by  $f(x) = \sin x$  and  $g(x) = \cos 2x$ .

- (a) Describe the single transformation of the graph of  $y = \cos x$  that will produce the graph of  $y = g(x)$ .

[2 marks]

**Question 8b**

- (b) On the same set of axes, sketch the graphs of  $y = f(x)$  and  $y = g(x)$  in the interval  $-\pi \leq x \leq 3\pi$ .

[4 marks]

**Question 8c**

- (c) By using an appropriate trigonometric identity to solve the equation  $\sin x = \cos 2x$  in the interval  $-\pi \leq x \leq 3\pi$ , determine the points of intersection of the two curves from your graph in part (b). Label those points on your graph.

[6 marks]



