

# **IB Physics DP**

# YOUR NOTES

#### 1. Measurement & Uncertainties

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#### 1.1 Measurements in Physics

#### 1.1.1 SI Units

#### SI Base Quantities

## International System (S.I.) Units

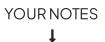
- There is a seemingly endless number of units in Physics
- These can all be reduced to seven base units from which every other unit can be derived
- These seven units are referred to as the SI Base Units; making up the system of measurement officially used in almost every country around the world

#### SI Base Quantities Table

QUANTITY	SI BASE UNIT	SYMBOL
MASS	KILOGRAM	kg
LENGTH	METRE	m
TIME	SECOND	s
CURRENT	AMPERE	А
TEMPERATURE	KELVIN	K
AMOUNT OF SUBSTANCE	MOLE	mol

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Six SI quantities are shown. The seventh quantity, the candela, measures luminous intensity, and is not covered in IB Physics. You may meet it later if you continue with Physics at university.





#### **Derived Units**

#### **Derived Units**

- Derived units are derived from the seven SI Base units
- The base units of physical quantities such as:
  - Newtons, N
  - Joules. J
  - Pascals, Pa, can be deduced
- To deduce the base units, it is necessary to use the definition of the quantity
- The Newton (N), the unit of force, is defined by the equation:
  - Force = mass x acceleration
  - $\circ$  N = kg x m s<sup>-2</sup> = kg m s<sup>-2</sup>
  - Therefore, the Newton (N) in SI base units is kg m s<sup>-2</sup>
- The Joule (J), the unit of energy, is defined by the equation:
  - Energy =  $\frac{1}{2}$  × mass × velocity<sup>2</sup>
  - $\circ$  J = kg × (m s<sup>-1</sup>)<sup>2</sup> = kg m<sup>2</sup> s<sup>-2</sup>
  - Therefore, the Joule (J) in SI base units is kg m<sup>2</sup> s<sup>-2</sup>
- The Pascal (Pa), the unit of pressure, is defined by the equation:
  - Pressure = force ÷ area
  - Pa = N  $\div$  m<sup>2</sup> = (kg m s<sup>-2</sup>)  $\div$  m<sup>2</sup> = kg m<sup>-1</sup> s<sup>-2</sup>
  - ∘ Therefore, the Pascal (Pa) in SI base units is **kg m**<sup>-1</sup> **s**<sup>-2</sup>

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#### 1.1.2 Using Scientific Notation

## Scientific Notation & Metric Multipliers

#### Scientific Notation

- In physics, measured quantities cover a large range from the very large to the very small
- Scientific notation is a form that is based on powers of 10
- The scientific form must have **one digit** in front of the decimal place
  - o Any remaining digits remain behind the decimal place
  - The magnitude of the value comes from multiplying by 10<sup>n</sup> where n is called 'the power'
  - This power is positive when representing large numbers or negative when representing small numbers



#### Worked Example

Express 4 600 000 in scientific notation.

#### Step 1: Write the convention for scientific notation

- To convert into scientific notation, only one digit may remain in front of the decimal point
  - Therefore, the scientific notation must be  $4.6 \times 10^{n}$
- $\circ$  The value of *n* is determined by the number of decimal places that must be moved to return to the original number (i.e. 4600000)

#### Step 2: Identify the number of digits after the 4

In this case, that number is +6

#### Step 3: Write the final answer in scientific notation

∘ The solution is: 4.6 × 10<sup>6</sup>

### Metric Multipliers

- When dealing with magnitudes of 10, there are **metric names** for many common quantities
- These are known as metric multipliers and they change the **size** of the **quantity** they are applied to
  - They are represented by prefixes that go in front of the measurement
- Some common examples that are well-known include
  - **kilo**metres, **k**m (× 10<sup>3</sup>)
  - centimetres, cm (x 10<sup>-2</sup>)
  - **milli**grams, **m**g ( $\times$  10<sup>-3</sup>)
- Metric multipliers are represented by a single letter symbol such as centi-(c) or Giga-(G)
  - o These letters go in front of the quantity of interest
  - o For example, centimetres (cm) or Gigawatts (GW)

#### Common Metric Multipliers Table

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PREFIX	ABBREVIATION	POWER OF TEN
TERA-	Т	10 <sup>12</sup>
GIGA-	G	10 <sup>9</sup>
MEGA-	М	10 <sup>6</sup>
KILO-	k	10 <sup>3</sup>
CENTI-	С	10 <sup>-2</sup>
MILLI-	m	10 <sup>-3</sup>
MICRO-	щ	10 <sup>-6</sup>
NANO-	n	10 <sup>-9</sup>
PICO-	þ	10 <sup>-12</sup>

YOUR NOTES



## Worked Example

What is the answer to the addition of 3.6 Mm + 2700 km in metres?

#### Step 1: Check which metric multipliers are in this problem

- M represents **Mega-** which is  $\times 10^6$  (not milli- which is small m!)
- k represents kilo- which is a multiplier of x 10<sup>3</sup>

#### Step 2: Apply these multipliers to get both quantities to be metres

$$3.6 \times 10^6 \text{ m} + 2.7 \times 10^6 \text{ m}$$

#### Step 3: Write the final answer in units of metres

$$6.3 \times 10^{6} \, \text{m}$$



## Exam Tip

You are expected to know metric multipliers for your exams. Make sure you become familiar with them in order to avoid any mistakes.



## **Significant Figures**

- Significant figures are the digits that accurately represent a given quantity
- Significant figures describe the precision with which a quantity is known
  - If a quantity has **more significant figures** then **more precise** information is known about that quantity

## Rules for Significant Figures

- Not all digits that a number may show are significant
- In order to know how many digits in a quantity are significant, these rules can be followed
  - Rule 1: In an integer, all digits count as significant if the last digit is non-zero
    - **Example:** 702 has 3 significant figures
  - Rule 2: Zeros at the end of an integer do not count as significant
    - **Example:** 705,000 has 3 significant figures
  - Rule 3: Zeros in front of an integer do not count as significant
    - **Example:** 0.002309 has 4 significant figures
  - **Rule 4:** Zeros at the end of a number less than zero count as significant, but those in front do not.
    - **Example:** 0.0020300 has 5 significant figures
  - Rule 5: Zeros after a decimal point are also significant figures.
    - **Example:** 70.0 has 3 significant figures
- Combinations of numbers must always be to the smallest number significant figures



## Worked Example

What is the solution to this problem to the correct number of significant figures:  $18 \times 384$ ?

#### Step 1: Identify the smallest number of significant figures

- 18 has only 2 significant figures, while 384 has 3 significant figures
- Therefore, the final answer should be to 2 significant figures

#### Step 2: Do the calculation with the maximum number of digits

 $18 \times 384 = 6912$ 

#### Step 3: Round to the final answer to 2 significant figures

 $6.9 \times 10^{3}$ 

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#### 1.1.3 Estimating Physical Quantities

## **Orders of Magnitude**

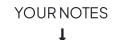
- When a number is expressed in an order of 10, this is an order of magnitude.
  - $\circ$  Example: If a number is described as  $3\times10^8$  then that number is actually  $3\times100\,000$  000
  - The order of magnitude of  $3 \times 10^8$  is just  $10^8$
- Orders of magnitude follows rules for rounding
  - The order of magnitude of  $6 \times 10^8$  is  $10^9$  as the magnitude is rounded up
- A quantity is an **order of magnitude larger** than another quantity if it is about **ten times larger**
- Similarly, two orders of magnitude would be 100 times larger, or  $10^2$ 
  - In physics, orders of magnitude can be very large or very small
- When estimating values, it's best to give the **estimate** of an order of magnitude to **the nearest power of 10** 
  - For example, the diameter of the Milky Way is approximately 1000 000 000 000
     000 000 000 m
- It is inconvenient to write this many zeros, so it's best to use **scientific notation** as follows:

- The order of magnitude is  $10^{21}$
- Orders of magnitude make it easier to compare the relative sizes of objects
  - $\circ$  For example, a quantity with an order of magnitude of  $10^6$  is  $10\,000$  times larger than a quantity with a magnitude of  $10^2$

#### **Estimating Physical Quantities Table**

Object of interest	Approximate length (m)	Order of magnitude (m)		
Distance to the edge of the observable universe	4.40 × 10 <sup>26</sup>	10 <sup>26</sup>		
Distance from Earth to Neptune	4.5 × 10 <sup>12</sup>	10 <sup>12</sup>		
Distance from London to Cape Town	9.7 × 10 <sup>6</sup>	10 <sup>7</sup>		
The length of a human	1.7	10°		
The length of an ant	9 × 10 <sup>-4</sup>	10 <sup>-3</sup>		
The length of a bacteria	2 × 10 <sup>-6</sup>	10 <sup>-6</sup>		

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## **Estimating Physical Quantities**

- To estimate is to obtain an approximate value
  - For **very** large or small quantities, using **orders of magnitudes** to estimate calculations is a valid approach
- Estimation is typically done to the nearest order of magnitude



## Worked Example

Estimate the order of magnitude of the following:

- a) The temperature of an oven (in Kelvin)
- b) The volume of the Earth (in m<sup>3</sup>)
- c) The number of seconds in a person's life if they live to be 95 years old

#### Part (a)

The temperature of the oven:

#### Step 1: Identify the approximate temperature of an oven

A conventional oven works at ~200 °C which is 473 K

#### Step 2: Identify the order of magnitude

- Since this could be written as  $4.73 \times 10^2$  K
- The order of magnitude is ~10<sup>2</sup>

#### Part (b)

The volume of the Earth (in  $m^3$ ):

#### Step 1: Identify the approximate radius of the Earth

• The radius of the Earth is  $\sim 6.4 \times 10^6$  m

#### Step 2: Use the radius to calculate the volume

• The volume of a sphere is equal to:

$$V = 4/3 \, \text{m} \, \text{r}^3$$

$$V = 4/3 \times \pi \times (6.4 \times 10^6)^3$$

$$V = 1.1 \times 10^{21} \,\mathrm{m}^3$$

#### Step 3: Identify the order of magnitude

■ The order of magnitude is ~10<sup>21</sup>

#### Part (c)

The number of seconds in 95 years:





#### Step 1: Find the number of seconds in a single year

1 year = 365 days with 24 hours each with 60 minutes with 60 seconds

 $365 \times 24 \times 60 \times 60 = 31536000$  seconds in a year

#### Step 2: Find the number of seconds in 95 years

 $95 \times 31536000 = 283824000$  seconds

- This is approximately 2.84 × 10<sup>8</sup> seconds
- Therefore the order of magnitude is  $\sim 10^8$



## Exam Tip

When studying IB DP Physics, it is recommended to state your answer on a single line explicitly (if possible) with all necessary details to ensure the examiners can mark correctly and for best practice.

#### 1.2 Uncertainties & Errors

#### 1.2.1 Random & Systematic Errors

## **Random & Systematic Errors**

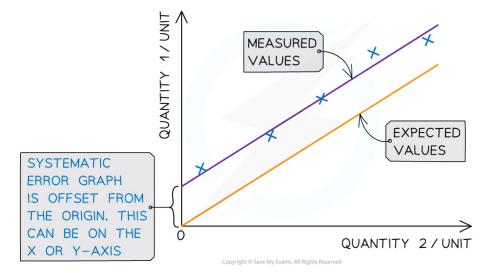
- Measurements of quantities are made with the aim of finding the true value of that quantity
  - In reality, it is impossible to obtain the true value of any quantity as there will always be a degree of **uncertainty**
- The uncertainty is an estimate of the difference between a **measurement reading** and the **true value**
- The two types of **measurement errors** that lead to uncertainty are:
  - Random errors
  - Systematic errors

#### Random Errors

- Random errors cause unpredictable fluctuations in an instrument's readings as a result of uncontrollable factors, such as environmental conditions
- This affects the precision of the measurements taken, causing a wider spread of results about the mean value
- To reduce random error:
  - Repeat measurements several times and calculate an average from them

#### Systematic Errors

- Systematic errors arise from the use of faulty instruments used or from flaws in the experimental method
- This type of error is repeated consistently every time the instrument is used or the method is followed, which affects the accuracy of all readings obtained
- To **reduce** systematic errors:
  - Instruments should be recalibrated, or different instruments should be used
  - o Corrections or adjustments should be made to the technique



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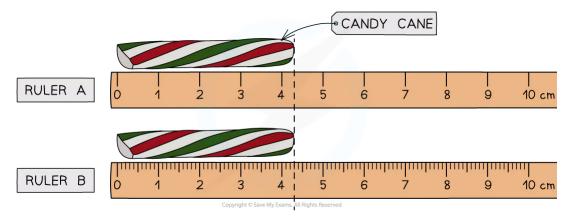
#### Systematic errors on graphs are shown by the offset of the line from the origin

#### **Zero Errors**

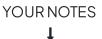
- This is a type of systematic error which occurs when an instrument gives a reading when the **true reading is zero** 
  - o For example, a top-ban balance that starts at 2 g instead of 0 g
- To account for zero errors
  - Take the **difference** of the **offset** from each value
  - For example, if a scale starts at 2 g instead of 0 g, a measurement of 50 g would actually be 50 - 2 = 48 g
  - The offset could be positive or negative

## **Reading Errors**

- When measuring a quantity using an **analogue** device such as a ruler, the uncertainty in that measured quantity is **±0.5** the smallest measuring interval
- When measuring a quantity using a **digital** device such as a digital scale or stopwatch, the uncertainty in that measured quantity is ±1 the smallest measuring interval
- To reduce reading errors:
  - Use a **more precise** device with **smaller measuring intervals** and therefore less uncertainty



Both rulers measure the same candy cane, yet Ruler B is more precise than Ruler A due to smaller interval size





#### 1.2.2 Calculating Uncertainties

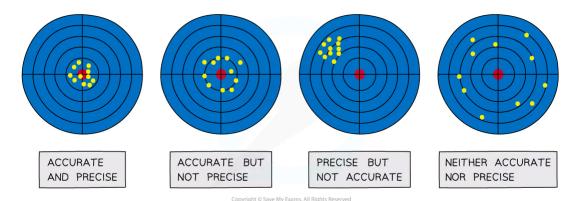
#### **Uncertainties**

#### Precision

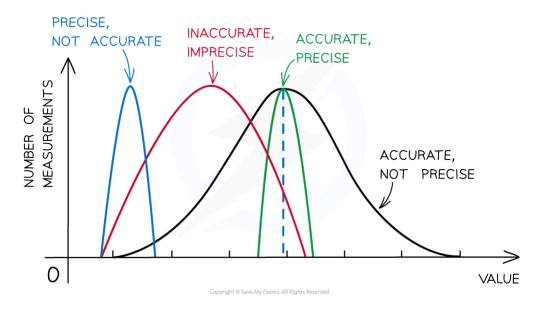
- Precise measurements are ones in which there is **very little spread** about the **mean** value, in other words, **how close** the measured values are **to each other**
- If a measurement is repeated several times, it can be described as **precise** when the values are **very similar to**, **or the same** as, each other
  - Another way to describe this concept is if the **random uncertainty** of a measurement is **small**, then that measurement can be said to be **precise**
- The precision of a measurement is reflected in the values recorded measurements to a greater number of decimal places are said to be more **precise** than those to a whole number

#### Accuracy

- A measurement is considered **accurate** if it is close to the true value
  - Another way to describe this concept is if the systematic error of a measurement is small, then that measurement can be said to be accurate
- The accuracy can be **increased by repeating measurements** and finding a mean of the results
- Repeating measurements also helps to identify anomalies that can be omitted from the final results



The difference between precise and accurate results



Representing precision and accuracy on a graph

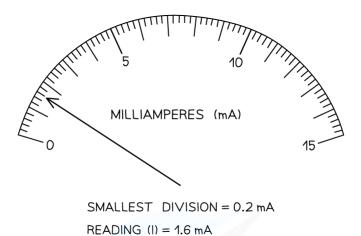
### Types of Uncertainty

- There is always a degree of uncertainty when measurements are taken; the uncertainty can be thought of as the difference between the **actual** reading taken (caused by the equipment or techniques used) and the true value
- Uncertainties are **not** the same as errors
  - Errors can be thought of as issues with equipment or methodology that cause a reading to be different from the true value
  - The uncertainty is a range of values around a measurement within which the true value is expected to lie, and is an **estimate**
- For example, if the true value of the mass of a box is 950 g, but a systematic error with a balance gives an actual reading of 952 g, the uncertainty is ±2 g
- These uncertainties can be represented in a number of ways:
  - Absolute Uncertainty: where uncertainty is given as a fixed quantity
  - Fractional Uncertainty: where uncertainty is given as a fraction of the measurement
  - Percentage Uncertainty: where uncertainty is given as a percentage of the measurement

percentage uncertainty = 
$$\frac{\text{uncertainty}}{\text{measured value}} \times 100\%$$

- To find uncertainties in different situations:
  - The uncertainty in a reading: ± half the smallest division
  - $\circ$  The uncertainty in repeated data: half the range i.e.  $\pm \frac{1}{2}$  (largest smallest value)
  - The uncertainty in digital readings: ± the last significant digit unless otherwise quoted





ABSOLUTE UNCERTAINTY ( $\Delta I$ ) =  $\frac{1}{2} \times 0.2 \text{ mA} = 0.1 \text{ mA}$  $I = 1.6 \pm 0.1 \text{ mA}$ 

FRACTIONAL UNCERTAINTY = 
$$\frac{\text{UNCERTAINTY}}{\text{VALUE}} = \frac{0.1}{1.6} = \frac{1}{16}$$

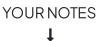
$$I = 1.6 \pm \frac{1}{16} \text{mA}$$

PERCENTAGE UNCERTAINTY (%) = 
$$\frac{\text{UNCERTAINTY}}{\text{VALUE}} \times 100 = \frac{0.1}{1.6} \times 100 = 6.2\%$$
  
I = 1.6 ± 6.2% mA

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#### How to calculate absolute, fractional and percentage uncertainty

• Always make sure your absolute or percentage uncertainty is to the same number of **significant figures** as the reading



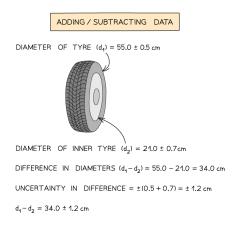
## **Propagating Uncertainties**

## **Combining Uncertainties**

• When combining uncertainties, the rules are as follows:

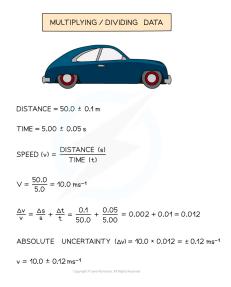
## Adding / Subtracting Data

• Add together the absolute uncertainties



## Multiplying / Dividing Data

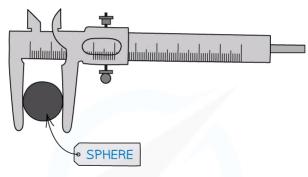
• Add the percentage or fractional uncertainties



## Raising to a Power

• Multiply the percentage uncertainty by the power

## RAISING TO A POWER



$$V = \frac{4}{3} \, \text{Tr}^3$$

$$r = 2.50 \pm 0.02$$
 cm

$$V = \frac{4}{3} \, \text{Tr} (2.50)^3 = 65.5 \, \text{cm}^3$$

$$\frac{\Delta V}{V} = 3 \times \frac{\Delta r}{r} = 3 \times \frac{0.02}{2.50} = 0.024$$

ABSOLUTELY UNCERTAINTY ( $\Delta V$ ) = 65.5 × 0.024 = 1.57cm<sup>3</sup>

PERCENTAGE UNCERTAINTY (% DV) = 100 × 0.024 = 2.4%

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## 2

## Worked Example

Consider two lengths:

 $A = 5.0 \pm 0.1$  cm and  $B = 2.5 \pm 0.1$  cm

Which of the following has the smallest percentage uncertainty

- **A**. A + B
- **B**. A B
- C. A×B
- D. A

#### Step 1: List the known quantities

- $\circ$  A = 5.0 cm
- Uncertainty in A, ΔA = 0.1 cm

- $\circ$  B = 2.5 cm
- ∘ Uncertainty in B, ΔB = 0.1 cm

#### Step 2: Check the percentage uncertainty of option A

$$A + B = 5.0 + 2.5 = 7.5 \text{ cm}$$

- $\circ$  The rule for propagating uncertainties for adding data (A + B) is  $\Delta$ A +  $\Delta$ B
- The combined uncertainties are:

$$0.1 + 0.1 = \pm 0.2 \, \text{cm}$$

• Therefore, the percentage uncertainty is:

$$(0.2 \div 7.5) \times 100 \approx 2.7\%$$

#### Step 3: Check the percentage uncertainty of option B

$$A - B = 5.0 - 2.5 = 2.5 cm$$

- $\circ$  The rule for propagating uncertainties for subtracting data (A B) is  $\Delta A + \Delta B$
- The combined uncertainties are:

$$0.1 + 0.1 = \pm 0.2 \, \text{cm}$$

• Therefore the percentage uncertainty is:

$$(0.2 \div 2.5) \times 100 = 8\%$$

#### Step 4: Check the percentage uncertainty of option C

$$A \times B = 5.0 \times 2.5 = 12.5 \text{ cm}$$

- The rule for propagating uncertainties for multiplying data (A  $\times$  B) is  $\Delta$ A/A +  $\Delta$ B/B
- The combined uncertainties are:

$$(0.1 \div 5.0) + (0.1 \div 2.5) = 0.02 + 0.04 = 0.06$$

• Therefore the percentage uncertainty is:

$$0.06 \times 100 = 6\%$$

#### Step 5: Check the percentage uncertainty of option D

- $\circ$  A = 5.0 cm and the uncertainty is 0.1 cm
- Therefore the percentage uncertainty is:

$$(0.1 \div 5.0) \times 100 = 2\%$$

#### Step 6: Compare and select the answer with the smallest percentage uncertainty

 Comparing the four options, option D is the correct answer as it has a value of 2% which is the smallest percentage uncertainty



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## Worked Example

For the value B = 3.0  $\pm$  0.1, if B is square rooted ( $\sqrt{B}$ ) what is the answer along with the absolute uncertainty?

Step 1: Find what the value of the quantity will be

$$\sqrt{B} = \sqrt{3.0} \approx 1.73$$

Step 2: Find the percentage uncertainty of the original

$$(0.1 \div 3.0) \times 100 \approx 3.33\%$$

Step 3: The percentage uncertainty needs to be multiplied by the power of the operation

$$3.33 \times (1 \div 2) \approx 1.67\%$$

Step 4: Apply the percentage uncertainty to the absolute answer

1.67% in decimal form is 0.0167. Therefore:  $0.0167 \times 1.73 \approx 0.03$ 

Step 5: State the complete answer

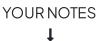
$$\sqrt{B} = 1.73 \pm 0.03$$



## Exam Tip

Remember:

- Absolute uncertainties (denoted by  $\Delta$ ) have the same units as the quantity
- Percentage uncertainties have no units
- The uncertainty in constants, such as  $\pi,$  is taken to be zero

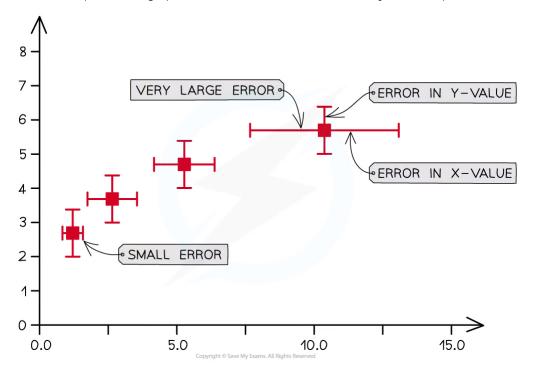




#### 1.2.3 Determining Uncertainties from Graphs

#### **Error Bars**

- The uncertainty in a measurement can be shown on a graph as an **error bar**
- This bar is drawn above and below the point (or from side to side) and shows the **uncertainty** in that measurement
- Error bars are plotted on graphs to show the **absolute uncertainty** of values plotted

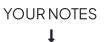


Representing error bars on a graph



## Exam Tip

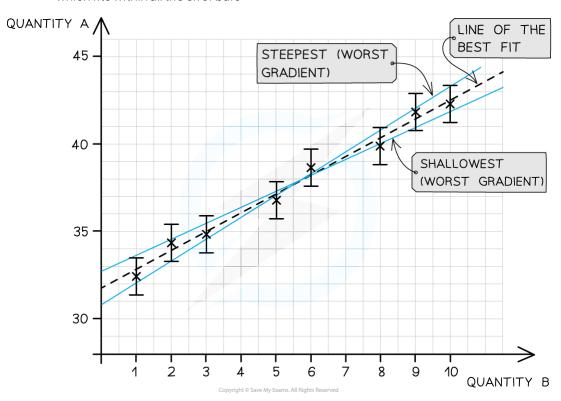
A common misconception is that error bars need to all be the same size. In physics, this is not the case and each data point can have different error bar sizes as they have different uncertainties.





## **Determining Uncertainties from Graphs**

- To calculate the **uncertainty in a gradient**, two lines of best fit should be drawn on the graph:
  - The 'best' line of best fit, which passes as **close** to the points **as possible**
  - The 'worst' line of best fit, either the **steepest possible** or the **shallowest possible** line which fits within all the error bars



# The line of best fit passes as close as possible to all the points. The steepest and shallowest lines are known as the worst fit

• The percentage uncertainty in the **gradient** can be found using the magnitude of the 'best' and 'worst' gradients:

$$\text{percentage uncertainty} = \frac{\textit{best gradient} - \textit{worst gradient}}{\textit{best gradient}} \times 100\%$$

- Either the steepest or shallowest line of best fit may have the 'worst' gradient on a case-by-case basis.
  - The 'worst' gradient will be the one with the **greatest difference** in magnitude from the 'best' line of best fit.
  - The equation **above** is for the case where the 'worst' gradient is the **shallowest**.
  - If the 'worst' gradient is the steepest, then the 'worst' gradient should be subtracted from the 'best' gradient and then divided by the best gradient and multiplied by 100
- Alternatively, the **average** of the two maximum and minimum lines can be used to calculate the percentage uncertainty:

1



percentage uncertainty = 
$$\frac{max.\ gradient-min.\ gradient}{2} \times 100\%$$



• The percentage uncertainty in the **y-intercept** can be found using:

percentage uncertainty = 
$$\frac{best\ y\ intercept - worst\ y\ intercept}{best\ y\ intercept} \times 100\%$$

percentage uncertainty =  $\frac{max.\ y\ intercept - min.\ y\ intercept}{2} \times 100\%$ 

## Percentage Difference

- The percentage difference gives an indication of how close the **experimental value** achieved from an experiment is to the **accepted value** 
  - It is **not** a percentage uncertainty
- The percentage difference is defined by the equation:

percentage difference = 
$$\frac{experimental\ value\ -\ accepted\ value\ }{accepted\ value\ } \times 100\%$$

- The experimental value is sometimes referred to as the 'measured' value
- The accepted value is sometimes referred to as the 'true' value
  - This may be labelled on a component such as the capacitance of a capacitor or the resistance of a resistor
  - o Or, from a reputable source such as a peer-reviewed data booklet
- For example, the acceleration due to gravity g is known to be 9.81 m s<sup>-2</sup>. This is its **accepted** value
  - $\circ$  From an experiment, the value of g may be found to be 10.35 m s<sup>-2</sup>
  - Its percentage difference would therefore be 5.5 %
- The smaller the percentage difference, the more accurate the results of the experiment



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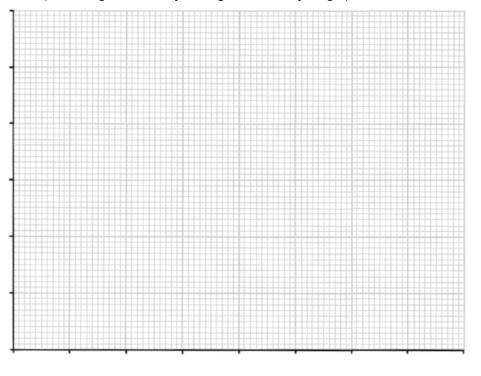
## Worked Example

On the axes provided, plot the graph for the following data and draw error bars and lines of best and worst fit.

Force / N	10	20	30	40	50	60	70	80
Extension / mm	8.5 ± 1	11 ± 0.5	15 ± 1	15 ± 2	20 ± 1.5	19.5 ± 2	22 ± 0.5	26±1

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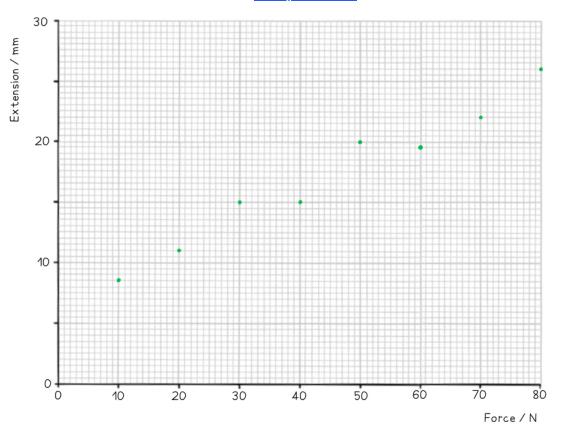
Find the percentage uncertainty in the gradient from your graph.



**Step 1:** Draw sensible scales on the axes and plot the data

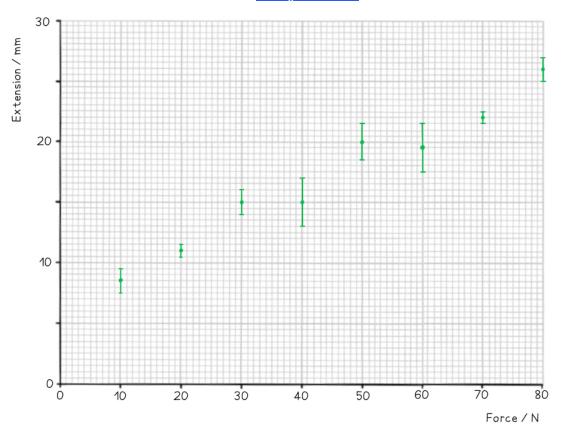






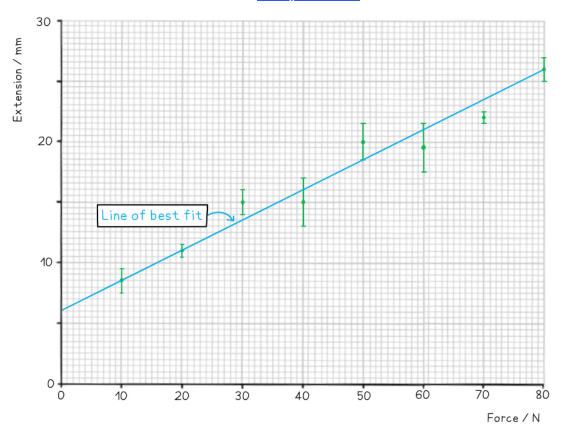
**Step 2:** Draw the errors bars for each point





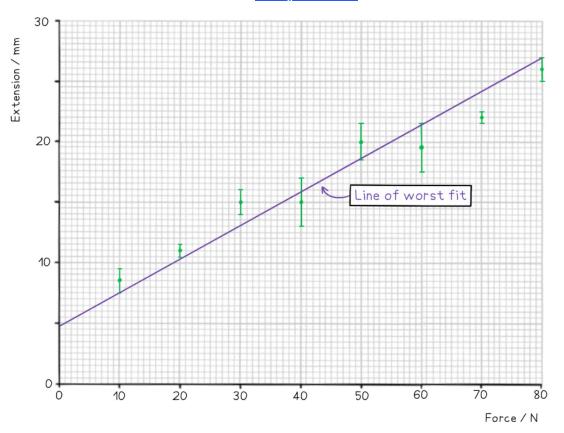
**Step 3:** Draw the line of best fit





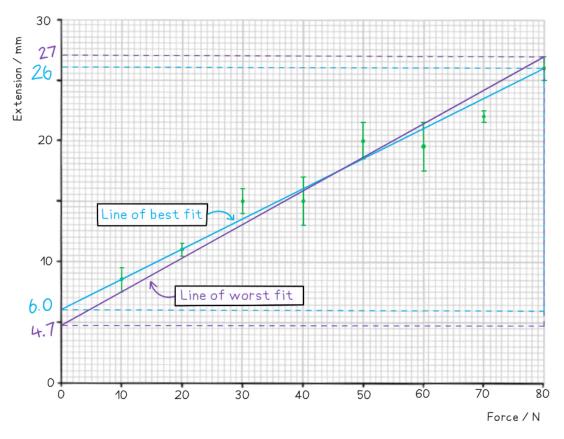
**Step 4:** Draw the line of worst fit





**Step 5**: Work out the gradient of each line and calculate the percentage uncertainty





Best gradient = 
$$\frac{\Delta y}{\Delta x} = \frac{26-6}{80-0} = 0.25$$

Worst gradient = 
$$\frac{\Delta y}{\Delta x} = \frac{27 - 4.7}{80 - 0} = 0.28$$

Percentage uncertainty = 
$$\frac{0.28 - 0.25}{0.25} \times 100\% = 12\%$$

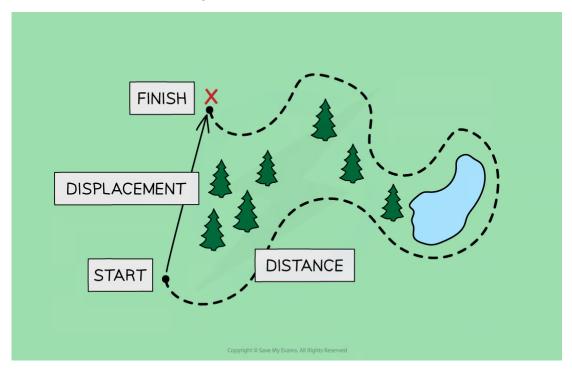


#### 1.3 Vectors & Scalars

#### 1.3.1 Vector & Scalar Quantities

#### **Vector & Scalar Quantities**

- A scalar is a quantity which only has a magnitude (size)
- A vector is a quantity which has both a magnitude and a direction
- For example, if a person goes on a hike in the woods to a location which is a couple of miles from their starting point
  - As the crow flies, their **displacement** will only be a few miles but the **distance** they walked will be much longer



#### Displacement is a vector while distance is a scalar quantity

- Distance is a scalar quantity
  - This is because it describes how an object has travelled overall, but not the direction it has travelled in
- Displacement is a vector quantity
  - This is because it describes how far an object is from where it started and in what direction
- Some common scalar and vector quantities are shown in the table below:

#### **Scalars and Vectors Table**





SCALARS	VECTORS
DISTANCE	DISPLACEMENT
SPEED	VELOCITY
MASS	ACCELERATION
TIME	FORCE
ENERGY	MOMENTUM
VOLUME	
DENSITY	
PRESSURE	
ELECTRIC CHARGE	
TEMPERATURE	



## Exam Tip

Do you have trouble figuring out if a quantity is a vector or a scalar? Just think - can this quantity have a minus sign? For example - can you have negative energy? No. Can you have negative displacement? Yes!





#### 1.3.2 Combining & Resolving Vectors

## **Combining & Resolving Vectors**

- Vectors are represented by an arrow
  - The arrowhead indicates the direction of the vector
  - The **length** of the arrow represents the **magnitude**

### **Combining Vectors**

- Vectors can be combined by **adding** or **subtracting** them to produce the **resultant vector** 
  - The **resultant vector** is sometimes known as the 'net' vector (eg. the net force)
- There are two methods that can be used to combine vectors: the **triangle method** and the **parallelogram method**
- To combine vectors using the triangle method:
  - Step 1: link the vectors head-to-tail
  - **Step 2:** the resultant vector is formed by connecting the tail of the first vector to the head of the second vector
- To combine vectors using the parallelogram method:
  - Step 1: link the vectors tail-to-tail
  - Step 2: complete the resulting parallelogram
  - Step 3: the resultant vector is the diagonal of the parallelogram

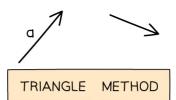


## Worked Example

Draw the vector c = a + b



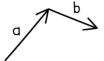


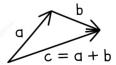


STEP 1: LINK THE VECTORS HEAD-TO-TAIL

STEP 2: FORM THE RESULTANT VECTOR FROM LINKING THE TAIL OF a TO THE HEAD OF b

YOUR NOTES



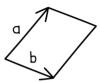


PARALLELOGRAM METHOD

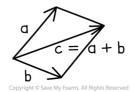
STEP 1: LINK THE VECTORS TAIL-TO-TAIL

STEP 2: COMPLETE THE RESULTING PARALLELOGRAM





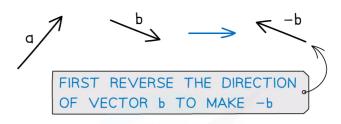
STEP 3: THE RESULTANT VECTOR
IS THE DIAGONAL OF THE PARALLELOGRAM



?

Worked Example

Draw the vector c = a - b

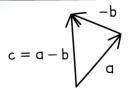


TRIANGLE METHOD

STEP 1: LINK THE VECTORS HEAD-TO-TAIL

STEP 2: FORM THE RESULTANT VECTOR BY LINKING THE TAIL OF a TO THE HEAD OF -b

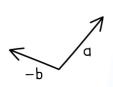


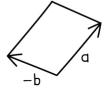


PARALLELOGRAM METHOD

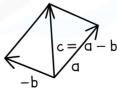
STEP 1: LINK THE VECTORS TAIL-TO-TAIL

STEP 2: COMPLETE THE RESULTING PARALLELOGRAM





STEP 3: THE RESULTANT VECTOR
IS THE DIAGONAL OF THE PARALLELOGRAM



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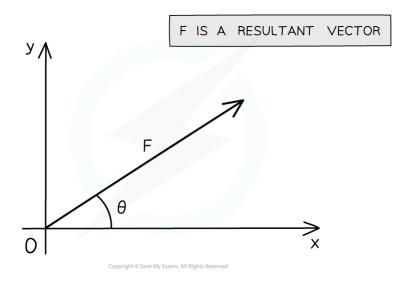
### **Resolving Vectors**

- Two vectors can be represented by a single **resultant vector** 
  - Resolving a vector is the opposite of adding vectors
- A single resultant vector can be resolved
  - This means it can be represented by **two** vectors, which in combination have the same effect as the original one

YOUR NOTES \$\frac{1}{4}\$

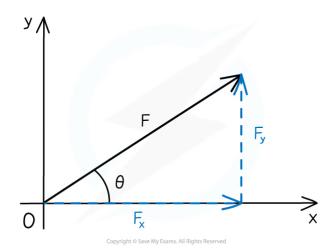


- When a single resultant vector is broken down into its **parts**, those parts are called **components**
- For example, a force vector of magnitude F and an angle of  $\theta$  to the horizontal is shown below



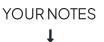
The resultant force F at an angle  $\theta$  to the horizontal

• It is possible to **resolve** this vector into its **horizontal** and **vertical** components using trigonometry



 $The \, resultant \, force \, F \, can \, be \, split \, into \, its \, horizontal \, and \, vertical \, components$ 

- For the **horizontal** component,  $F_x = F \cos \theta$
- For the **vertical** component,  $F_y = F \sin \theta$



**YOUR NOTES** 

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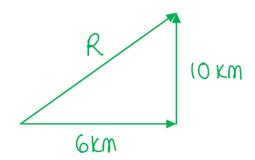


## Worked Example

A hiker walks a distance of 6 km due east and 10 km due north.

Calculate the magnitude of their displacement and its direction from the horizontal.

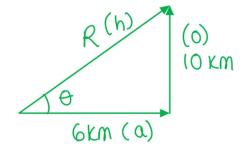
Step 1: Draw a vector diagram



Step 2: Calculate the magnitude of the resultant vector using Pythagoras' Theorem

$$R = \sqrt{6^2 + 10^2} = 2\sqrt{34}$$

Step 3: Calculate the direction of the resultant vector using trigonometry



$$tan(\theta) = \frac{opposite}{adjacent} = \frac{10}{6}$$

$$\theta = \tan^{-1}\left(\frac{10}{6}\right) = 59^{\circ}$$

Step 4: State the final answer complete with direction



 $R = 2\sqrt{34} = 11.66 = 12 \text{ km}$ 

 $\theta$  = **59°** east and upwards from the horizontal



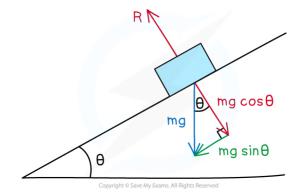
#### 1.3.3 Solvina Vector Problems

## **Solving Vector Problems**

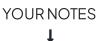
- In physics, vectors appear in many different topic areas
  - Specifically, vectors are often combined and resolved to solve problems when considering motion, forces, and momentum

#### Forces on an Inclined Plane

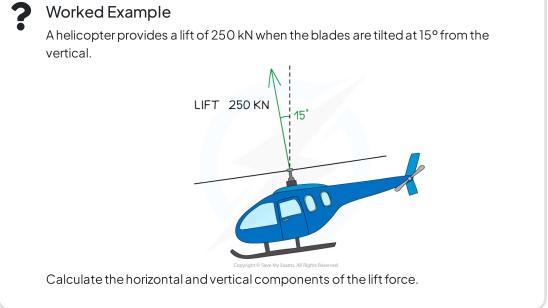
- Objects on an inclined plane is a common scenario in which vectors need to be resolved
   An inclined plane, or a slope, is a flat surface tilted at an angle, θ
- Instead of thinking of the component of the forces as horizontal and vertical, it is easier to think of them as **parallel** or **perpendicular** to the slope
- The **weight** of the object is vertically downwards and the **normal** (or reaction) force, *R* is always vertically up from the object
- The weight W is a vector and can be split into the following components:
  - $W\cos(\theta)$  perpendicular to the slope
  - $\circ$  W sin ( $\theta$ ) parallel to the slope
- If there is no friction, the force  $W \sin(\theta)$  causes the object to move down the slope
- If the object is not moving perpendicular to the slope, the normal force will be  $R = W \cos(\theta)$



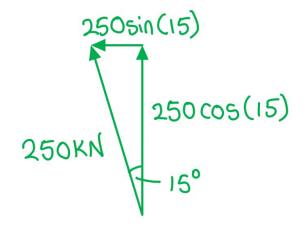
The weight vector of an object on an inclined plane can be split into its components parallel and perpendicular to the slope



YOUR NOTES



Step 1: Draw a vector triangle of the resolved forces



Step 2: Calculate the vertical component of the lift force

 $Vertical = 250 \times cos(15) = 242 \text{ kN}$ 

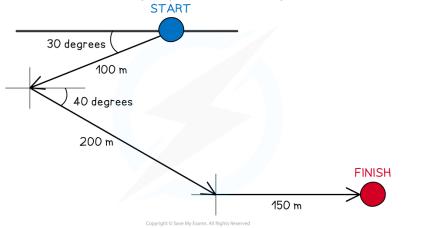
Step 3: Calculate the horizontal component of the lift force

Horizontal =  $250 \times \sin(15) = 64.7 \text{ kN}$ 



### Worked Example

A person is exploring a new part of town, from their starting point they walk 100 m in the direction 30.0° South of West. They then walk 200 m in the direction 40.0° degrees South of East and finally they walk 150 m directly East.



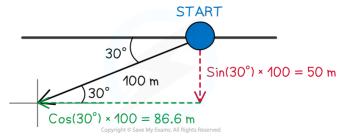
Calculate the magnitude of their displacement from their original position.

In order to calculate the answer, the vectors of displacement must be resolved into their x-components and y-components and then combined. In this case, this effectively means the x-direction is East-West and the y-direction is North-South

#### Step 1: Consider positive and negative directions for reference

- Since East is likely to be larger consider it the positive displacement and West as negative
- Similarly, consider South as positive and North as negative

Step 2: Resolve the first displacement (100 m magnitude) into its components



• The horizontal component can be resolved from:

$$cos(30^{\circ}) \times 100 = 86.6 \,\mathrm{m}$$

- o This is in a Western (negative horizontal) direction
- The vertical component can be resolved from:

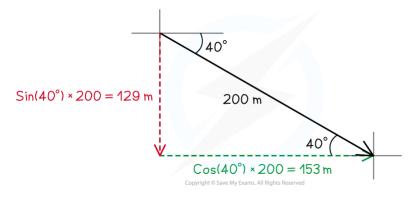
$$\sin(30^{\circ}) \times 100 = 50.0 \text{ m}$$

• This is in a Southern (positive vertical) direction

**YOUR NOTES** 

1

Step 3: Resolve the second displacement (200 m magnitude) into its components



• The horizontal component can be resolved from:

$$cos(40^{\circ}) \times 200 = 153 \text{ m}$$

- This is in an Eastern (positive horizontal) direction
- The vertical component can be resolved from:

$$\sin(40^\circ) \times 200 = 129 \,\mathrm{m}$$

• This is in a Southern (positive vertical) direction

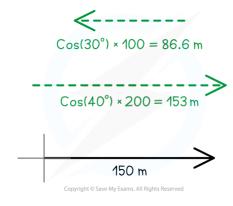
#### Step 4: Resolve the third displacement (150 m magnitude) into its components

• The horizontal component is already resolved into

150 m

- This is in an Eastern (positive horizontal) direction
- There is no vertical component for this vector

#### Step 5: Combine the horizontal (East-West) components

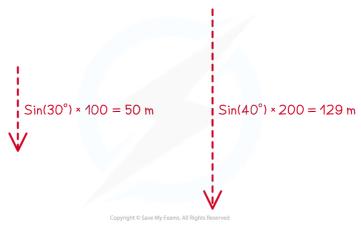


 $153 + 150 - 86.6 = 166 \,\mathrm{m}$ 

o This is in an Eastern (positive horizontal) direction

Step 6: Combine the vertical (North-South) components





 $50.0 + 129 = 170 \,\mathrm{m}$ 

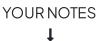
• This is in a Southern (positive vertical) direction

Step 7: Using Pythagoras theorem to find the resultant hypotenuse vector

$$\sqrt{(166^2 + 179^2)} = 244 \,\mathrm{m}$$

## Equilibrium

- Coplanar forces can be represented by vector triangles
- Forces are in equilibrium if an object is either
  - At rest
  - Moving at constant velocity
- In equilibrium, coplanar forces are represented by **closed** vector triangles
  - The vectors, when joined together, form a closed path
- The most common forces on objects are
  - Weight
  - Normal reaction force
  - Tension (from cords and strings)
  - Friction
- The forces on a body in equilibrium are demonstrated below:

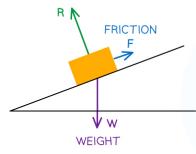


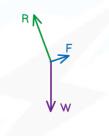


A VEHICLE IS AT REST ON A SLOPE AND HAS THREE FORCES ACTING ON IT TO KEEP IT IN EQUILIBRIUM

YOUR NOTES









STEP 1: DRAW ALL THE FORCES ON THE FREE-BODY DIAGRAM STEP 2:
REMOVE THE OBJECT
AND PUT ALL THE
FORCES COMING FROM
A SINGLE POINT

STEP 3:
REARRANGE THE FORCES
INTO A CLOSED VECTOR
TRIANGLE.
KEEP THE SAME LENGTH
AND DIRECTION

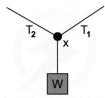
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#### Three forces on an object in equilibrium form a closed vector triangle



## Worked Example

A weight hangs in equilibrium from a cable at point  $\mathbf{X}$ . The tensions in the cables are  $T_1$  and  $T_2$  as shown.



Which diagram correctly represents the forces acting at point  $\mathbf{X}$ ?



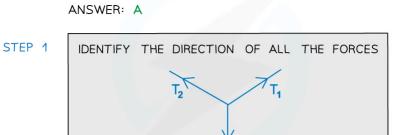


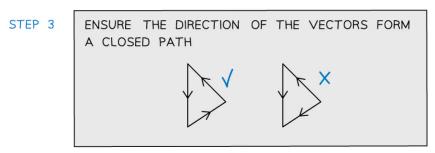




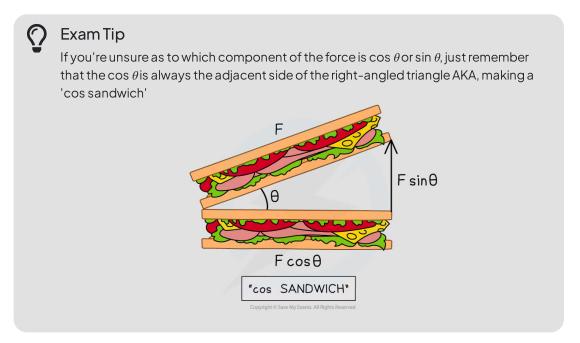
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YOUR NOTES





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