

1.1 Number Toolkit

Question Paper

Course	DPIB Maths
Section	1. Number & Algebra
Topic	1.1 Number Toolkit
Difficulty	Hard

Time allowed: 50
Score: /36
Percentage: /100

Question 1a

$$\text{Let } P = \frac{(4 \sin 2q - 2)(6 \tan q + 2)}{10(r + s)^2}, \text{ where } q = \frac{\pi}{6}, r = 6 \text{ and } s = 2.$$

(a) Calculate the exact value of P .

[4 marks]

Question 1b

(b) Give your answer from part (a) correct to

- (i) two decimal places
- (ii) two significant figures.

[2 marks]

Question 2a

$$\text{Let } W = \frac{(2 \cos 2x + y)(\tan \frac{x}{2} - z)}{10(5 \sin x + z^2)}, \text{ where } x = \frac{\pi}{2}, y = -1 \text{ and } z = 2.$$

(a) Find the value of W . Give your answer as a fraction.

[4 marks]

Question 2b

(b) Give your answer from part (a) to

- (i) three decimal places
- (ii) three significant figures.

[2 marks]

Question 3a

A prism has a cross sectional area of $5.50 \times 10^3 \text{ cm}^2$ and volume of $4.40 \times 10^4 \text{ cm}^3$.

(a) Calculate the length of the prism.

[3 marks]

Question 3b

The cross-sectional area of the prism is in the shape of a trapezium and its parallel sides measure 2 m and 2.4 m.

(b) Calculate the height of the trapezium. Give your answer in cm.

[3 marks]

Question 4a

Mary has found the exact answer for R is $\frac{45}{16}$.

(a) Write down the exact answer of R as a decimal.

[3 marks]

Question 4b

(b) Give your answer from part (a) correct to

- (i) three decimal places
- (ii) one significant figure.

[2 marks]

Question 5a

It is given that $\sin a = \frac{\sqrt{3}}{2}$ and $\sin b = \frac{1}{2}$, where $a \leq 180^\circ$ and $b \leq 180^\circ$.

(a) Find the size of the angles a and b .

[2 marks]

Question 5b

A circle has radius r equal to $\sqrt{\frac{\sin a}{\sin b}}$ cm.

(b) Find the exact value of the area of the circle, giving your answer in terms of π .

[4 marks]

Question 6a

A medium rare steak should have an internal temperature of 55°C to 56°C . Max decides to go to 10 different steak houses, he measures the internal temperature of a medium rare steak at each establishment and records the following:

51.0, 52.1, 62.9, 49.0, 59.8, 50.2, 54.3, 47.7, 48.6, 65.4

(a) Find the mean internal temperature of Max's recordings.

[1 mark]

Question 6b

Max goes to 5 more steak houses and calculates the mean of all 15 restaurants to be 55.2°C .

(b) Calculate the mean internal temperature from the 5 additional steak houses Max went to.

[3 marks]

Question 6c

Max records one last steak that has an internal temperature of T °C.

(c) Calculate the interval of T such that the mean internal temperature for all 16 steaks is within the temperature range for a medium rare steak.

[3 marks]