

1.1 Number Toolkit

Question Paper

Course	DP IB Maths
Section	1. Number & Algebra
Торіс	1.1 Number Toolkit
Difficulty	Very Hard

Time allowed:	70
Score:	/55
Percentage:	/100

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Question la

Consider the numbers $a = 11\sqrt{2}, b = (5 + 6\pi), c = \sqrt{2}, d = 6(\pi - 1).$

(a) Giving your answer to 1 decimal place, calculate the value of

- (i) *a*.
- (ii) *b*.
- (iii) *c*.
- (iv) *d*.

[2 marks]

Question 1b

Points P and Q have coordinates (a, b) and (c, d) respectively.

The formula for the distance, d, between two points with coordinates (x_1, y_1) and (x_2, y_2) is given in your formula booklet.

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

(b) Using your answers from part (a), calculate the distance, *d*, between points P and Q. Give your answer correct to 1 decimal place.



Question 1c

(c) Find the percentage error between the distance, correct to 1 decimal place, found in part (b) and the exact distance between points P and Q.

[4 marks]

Question 2a

Let $Y = (pq)^{-1}r$ and $T = pqr^{-1}$, where $p = \sin 60^{\circ}$, $q = \sqrt{3}$, r = 2

(a) Giving your answer to 1 decimal place, calculate the value of

- (i) *Y*.
- (ii) *T*.

[2 marks]

Question 2b

(b) Using your answers to part (a), estimate the value of *YT*. Give your answer as a fraction.

[1 mark]



Question 2c

(c) Calculate the percentage error between your estimated value of *YT* found in part (b) and the exact value of *YT*.

[4 marks]

Question 3a

A cuboid has length, l = 0.102 m, width, w = 9.4 cm and height, h = 0.25 m.

(a) Calculate the exact volume of the cuboid

- (i) in cm^3 .
- (ii) in m^3 .

[2 marks]

Question 3b

(b)Write your answers to part (a) (i) and (ii) in the form $a \times 10^k$, where $1 \le a < 10$, $k \in \mathbb{Z}$.



Question 3c

William estimates the volume of the cuboid as being $Q \text{ cm}^3$ and the percentage error in his estimate is 5%.

(c) Calculate the exact possible values of *Q*.

[4 marks]

Question 4a

Let $S = (a \sin^2 4b)(c^2 \tan^2 12d)^{-1} (\sqrt{a} + c - \cos 48b)$, where $a = 16, b = 7.5^\circ, c = 3$ and $d = 5^\circ$.

Note: $\sin^2\theta = (\sin\theta)^2$

(a) Find the value of *S*, giving your answer as a fraction.

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Question 4b

Let
$$X = \frac{\sqrt{a} + c^2 - 2\sin 54d}{\sqrt{a^3} - a - c}$$

(b) Find the value of *X*, giving your answer as a fraction.

[2 marks]

[2 marks]

Question 4c

(c) Calculate the value of *SX*, giving your answer as a fraction.

Question 4d

John estimates the value of *SX* to be 0.3.

(d)Calculate the percentage error in John's estimate.

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Question 5a

Consider the numbers $p = 2.41 \times 10^4$ and $q = 4.12 \times 10^5$.

(a) Giving your answers in the form $a \times 10^k$, where $1 \le a < 10, k \in \mathbb{Z}$, calculate

- (i) *p* + *q*
- (ii) *p* − *q*
- (iii) q p
- (iv) $\frac{p}{q}$

[4 marks]

Question 5b

The formula for the distance, *d*, between two points with coordinates (x_1, y_1) and (x_2, y_2) is given in your formula booklet.

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

(b) Using your answers to part (a), estimate the distance between points A(p + q, p - q) and $B(q - p, \frac{p}{q})$.



Question 5c

(c) Calculate the percentage error between the estimate of the distance between points P and Q found in part (b) and the exact distance.

[4 marks]

Question 6a

A shop sells bags of potatoes labelled as "5 kg". The shop owner weighs five bags, in kilograms, at random and recorded the following:

4.96, 4.89, 5.07, 5.11, 5.02

- (a) (i) Find the mean of the shop owner's recorded weights.
 - (ii) Calculate the percentage error between the mean and the stated weight of 5 kg.

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Question 6b

The shop owner shares his findings with his potato supplier, who weighs another five bags and recorded the following:

5.05, 5.01, 4.97, 5.09, X

The supplier allows a maximum percentage error of 1%.

(b) Find the interval for the values of X such that the percentage error from the five bags that the supplier weighed is less than 1%.

[3 marks]

Question 6c

(c) Find the interval for the values of X such that the percentage error from all the ten bags weighed is less than 1%.

[3 marks]

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Question 7

Solve the following systems of linear equations using technology.

(i)

$$2x - 5y - 7z = -21$$
$$3z + x - 4y = 44$$
$$x + z - y = 12$$

(ii)

$$z - x - y = -11$$

$$5x + 11z - 2y = -28$$

$$3y - 4z + x = 30$$

[6 marks]

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