

# 4.3 Probability

## Question Paper

Course	DPIB Maths
Section	4. Statistics & Probability
Topic	4.3 Probability
Difficulty	Hard

**Time allowed:** 90  
**Score:** /67  
**Percentage:** /100

**Question 1a**

A game is played using a fair spinner with four sectors numbered 1 to 4, as well as a fair dice with its six sides numbered 1 to 6.

- (a) Using an appropriate representation, describe the sample space of possible outcomes when the spinner is spun and the dice is rolled at the same time.

[3 marks]

**Question 1b**

When the game is played, the spinner is spun and the dice is rolled at the same time, and the player's score is defined to be the (positive) difference between the two results.

- (b) Find the probability of the score in the game being
- (i) exactly 0
  - (ii) 3 or more
  - (iii) a prime number

[4 marks]

**Question 1c**

The game is played 150 times.

(c) Find the expected number of times that a prime number score will occur.

[2 marks]

**Question 2a**

A survey was carried out of residents of a particular town, to find out what their preferred activity was when coronavirus lockdown restrictions were in place. Five hundred residents were surveyed, and the results are shown in the table below:

		Preferred activity				
		Daydreaming	Staring at phone	Exercising	Playing chess	Other
Age	13-17	11	37	33	1	2
	18-30	2	45	40	1	1
	31-54	33	8	31	21	8
	55-70	31	35	30	11	10
	>70	34	17	38	13	7

(a) One of the surveyed residents is selected at random. Given that the resident did not give a response of 'Other' to the survey, find the probability that this resident

- (i) preferred playing chess during lockdown
- (ii) was less than 55 years old and did not prefer daydreaming during lockdown.

[3 marks]

**Question 2b**

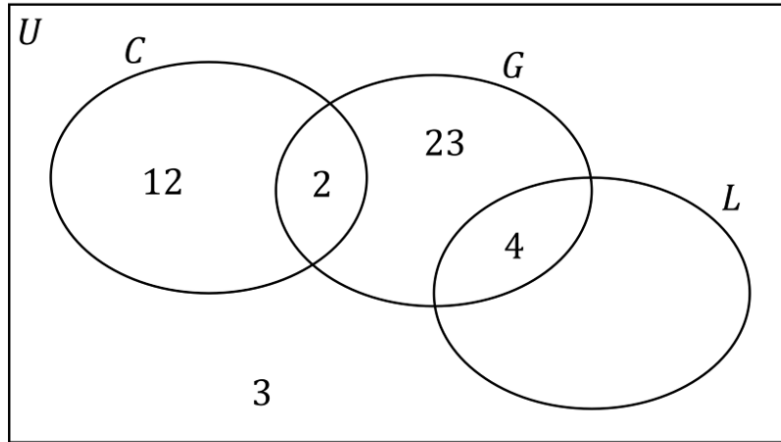
The town has a total population of 23681.

- (b) Assuming that the survey figures are representative of the town as a whole, estimate the number of residents of the town who
- (i) preferred daydreaming, exercising, staring at their phone or playing chess during lockdown
  - (ii) were between 31 and 70 years old and did not prefer exercising during lockdown.

[3 marks]

**Question 3a**

The Venn diagram displays information about the number of students taking each of three languages: Mandarin Chinese ( $C$ ), German ( $G$ ) and Latin ( $L$ ).



There are fifty students in total.

(a) Determine the number of students who take only Latin.

[2 marks]

**Question 3b**

A student is randomly chosen from the group.

(b) Find the probability that

- (i) the student studies German or Latin
- (ii) the student studies neither Mandarin Chinese nor Latin
- (iii) the student studies Mandarin Chinese, given that they study German
- (iv) the student studies Latin, given that they study Mandarin Chinese
- (v) the student studies Latin, given that they do not study German.

[10 marks]

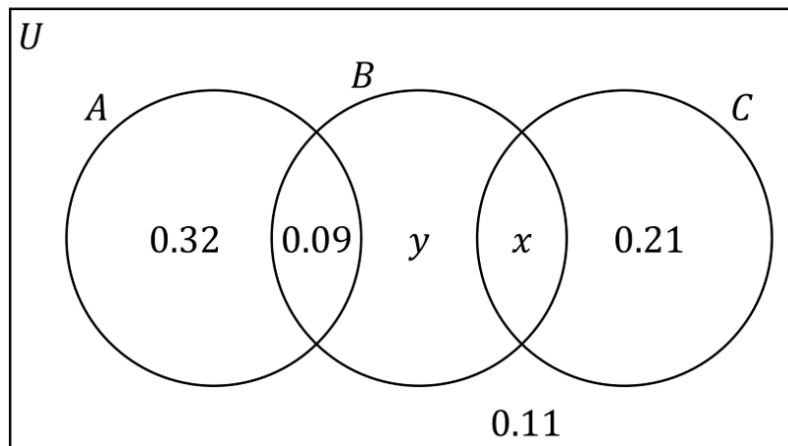
**Question 4a**

The Venn diagram illustrates the probabilities of members of a costumed performers' union having dressed as one or another superhero during a performance.

$A$  represents the event that the member has dressed as Aquaman.

$B$  represents the event that the member has dressed as Batman.

$C$  represents the event that the member has dressed as Captain Marvel.



Given that the probability of a member having dressed as Captain Marvel is 0.44,

(a) determine the values of

(i)  $x$

(ii)  $y$ .

[3 marks]

**Question 4b**

264 of the union's members have dressed as exactly two of the three superheroes.

(b) Use this information to determine the total number of members of the union.

[2 marks]

**Question 5**

$A$  and  $B$  are events such that  $P(A) = 0.24$ ,  $P(B) = 0.73$ , and  $P(A \cup B) = 0.84$ .

By drawing a Venn diagram to illustrate these probabilities, find

(i)  $P(A' \cup B)$

(ii)  $P(A \cap B')$

(iii)  $P((A \cap B)')$

[6 marks]



**Question 6**

$A$  and  $B$  are independent events, such that  $P(A) = 0.25$  and  $P(B) = 0.52$ .  $C$  is another event, such that  $B$  and  $C$  are mutually exclusive and  $P(A \cap C) = 0.09$ .

Given that  $P(A \cup B \cup C) = 0.95$ , find

(i)  $P(A \cap B)$

(ii)  $P(C)$

(iii)  $P(A' \cap B')$

(iv)  $P(A|C')$

[9 marks]

**Question 7a**

A bag contains 12 red marbles, 7 green marbles and 1 black marble. Two marbles are drawn from the bag without replacement.

- (a) Draw a tree diagram to illustrate the process described above, showing clearly the probabilities on each branch.

[3 marks]

**Question 7b**

(b) Find the probability that

- (i) the two marbles drawn are not both the same colour
- (ii) both marbles are green, given that both marbles drawn are the same colour.

[5 marks]

**Question 7c**

(c) In the context of the question, give an example of two mutually exclusive events. Be sure to justify that they are mutually exclusive.

[2 marks]

**Question 8a**

In a game of Unicorns Versus Zombies your unicorn is attempting to use the magic of its horn to dispel a cloud of zombie apocalypse flies. On the first attempt, the probability of the magic working is 0.7. If the magic works, then there is a probability of 0.2 that the flies will be turned into glitter pixies and join your rainbow army, otherwise the flies will simply be dispelled. If the magic does not work the first time you may try again, although the probability of your magic working the second time is only 0.6. Similarly, if your magic does not work the second time you may try a third time, but on the third attempt the probability of your magic working is reduced to 0.5. If your magic works on the second or third attempts the probabilities of dispelling the flies or turning them into glitter pixies are the same as for the magic working on the first attempt. If your magic does not work on the third attempt, however, then your unicorn is turned into an evil zombiecorn and joins the zombie horde. In all cases, the game ends when either the flies are turned into glitter pixies, or the flies are dispelled, or your unicorn is turned into a zombiecorn.

- (a) Draw a tree diagram to illustrate the above question, showing clearly the probabilities on each branch.

[4 marks]

**Question 8b**

(b) Find the probability that

- (i) the flies are turned into glitter pixies
- (ii) the flies are dispelled
- (iii) your unicorn is turned into a zombiecorn.

[3 marks]

**Question 8c**

(c) Explain why the events “the flies are turned into glitter pixies” and “the magic worked on the second attempt” are not independent events.

[3 marks]