

# 2.2 Quadratic Functions & Graphs

## Question Paper

Course	DPIB Maths
Section	2. Functions
Topic	2.2 Quadratic Functions & Graphs
Difficulty	Medium

**Time allowed:** 70  
**Score:** /53  
**Percentage:** /100

**Question 1a**

The curve  $C$  has equation  $y = x^2 - 3x + 2$ .

(a) Find the coordinates of any points where  $C$  intersects the coordinate axes.

[3 marks]

**Question 1b**

(b) Sketch the graph of  $C$ , showing clearly all points of intersection with the coordinate axes.

[3 marks]

**Question 2a**

(a) Write the quadratic function  $y = x^2 + 8x - 9$  in the form  $y = a(x + b)^2 + c$  where  $a$ ,  $b$  and  $c$  are integers to be found.

[2 marks]

**Question 2b**

(b) Write down the minimum point on the graph of  $y = x^2 + 8x - 9$ .

[1 mark]

**Question 2c**

(c) Sketch the graph of  $y = x^2 + 8x - 9$ , clearly labelling the minimum point and any point where the graph intersects the coordinate axes.

[3 marks]

**Question 3a**

(a) Solve the equation  $2x^2 + x - 6 = 0$ .

[2 marks]

**Question 3b**

(b) Find the coordinates of the turning point on the graph of  $y = 2x^2 + x - 6$ .

[3 marks]

**Question 3c**

(c) Sketch the graph of  $y = 2x^2 + x - 6$ , labelling the turning point and any points where the graph crosses the coordinate axes.

[2 marks]

**Question 4a**

(a) Find the minimum value of the function  $f(x) = x^2 + 4x + 5$ .

[3 marks]

**Question 4b**

(b) Hence, or otherwise, prove that the function  $f(x) = x^2 + 4x + 5$  has no real roots.

[2 marks]

**Question 5**

The function  $f(x) = kx^2 + 2kx - 3$  has two distinct real roots.

Show that  $k < -3$  or  $k > 0$ .

[3 marks]

**Question 6**

The equation  $2x^2 - 4x + 3 - 2k = 0$  has real roots.

Find the possible values of  $k$ .

[3 marks]

**Question 7**

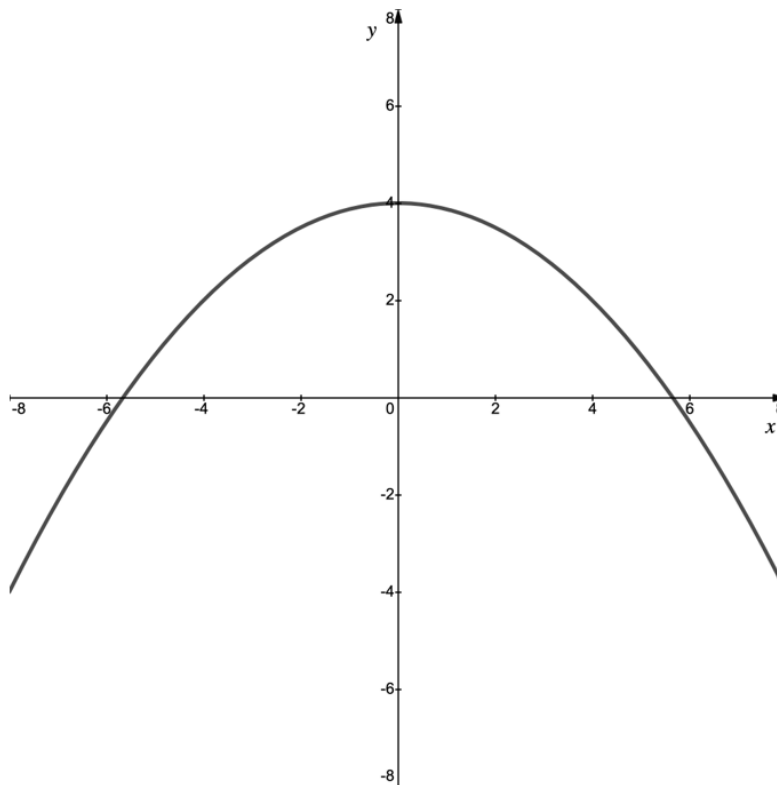
The equation  $y = x^2 + px + q$  has no real roots. Show that  $p^2 < 4q$ .

[2 marks]

**Question 8a**

The graph below shows the curve  $f(x) = 4 - \frac{x^2}{8}$ .

The curve is to be used as the model for the arch on a bridge where the water level under the bridge is represented by the  $x$ -axis. All measurements are in meters.



(a) Write down the maximum height of the bridge above the water.

[1 mark]

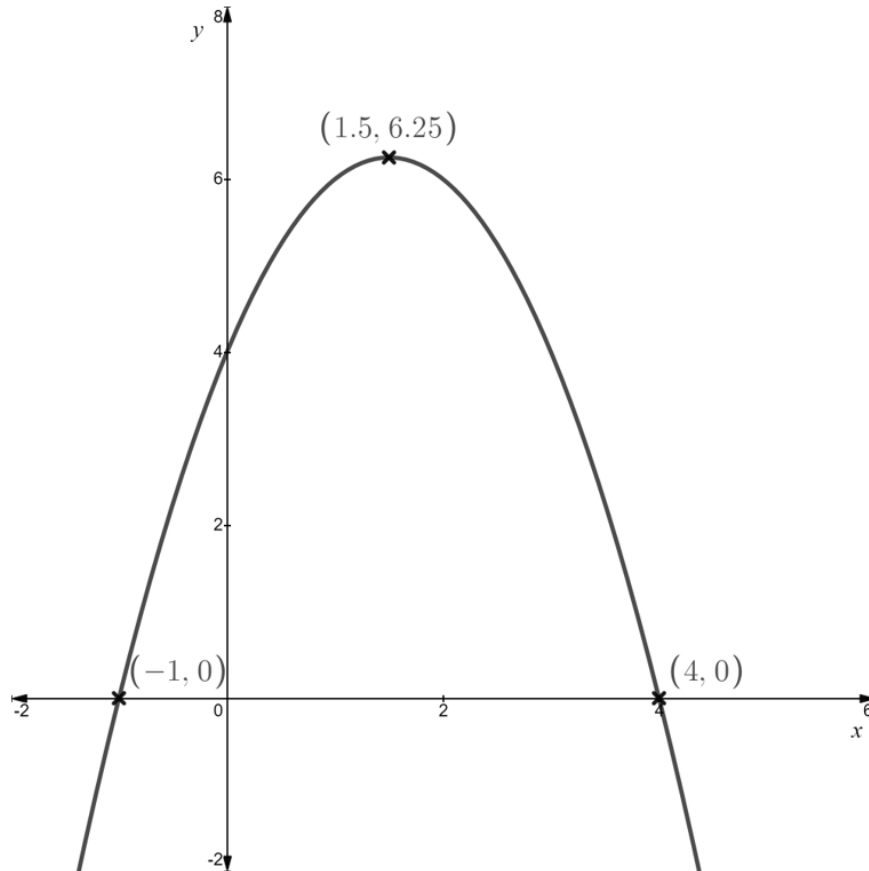
**Question 8b**

(b) Show that the bridge is wide enough to span a river of width 11m.

[3 marks]

**Question 9a**

The diagram below shows the graph of  $y = f(x)$ , where  $f(x)$  is a quadratic function. The intercepts with the  $x$ -axis and the turning point have been labelled.



(a) Write down the equation of the axis of symmetry for the graph of  $y = f(x)$ .

[1 mark]

**Question 9b**

(b) The function  $f(x)$  can be written in the form of  $f(x) = a(x - h)^2 + k$ . Find the values of  $a$ ,  $h$  and  $k$ .

[3 marks]



**Question 10**

Solve the equation  $x^4 - 13x^2 + 36 = 0$ .

[3 marks]

**Question 11**

Solve  $x^{\frac{2}{5}} + x^{\frac{1}{5}} = 6$ .

[4 marks]

**Question 12a**

Let  $f(x) = 2px^2 + (2p - 5)x + p - \frac{5}{2}$ , for  $x \in \mathbb{R}$ , where  $p \in \mathbb{Q}$ .

(a) Show that the discriminant of  $f$  is  $-4p^2 + 25$ .

[3 marks]

**Question 12b**

(b) Find the values of  $p$  so that the function  $f(x)$  has two **distinct** roots.

[3 marks]